Statistics – A

Summer term 2023

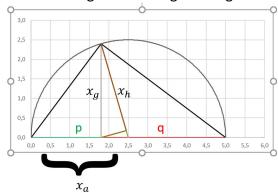
Exercise 1

1) A country exhibits the following distribution of educational qualifications

| Approved higher educational level | | |
|-----------------------------------|--------|--------|
| | Gender | |
| Sector of Qualification | Men | Female |
| Industrial | 5256 | 982 |
| Agricultural | 3221 | 432 |
| Public | 1001 | 602 |
| Financial | 2231 | 1820 |
| Trade | 872 | 1512 |

- a) Calculate the relative probabilities, the marginal distributions and provide the contingency table.
- b) Compare the descriptive result with the theoretical probabilities. Are the attributes statistically independent?
- c) Calculate the conditional probabilities of P(Gender|Sector of Qualification) and P(Sector of Qualification|Gender).
- Show for two numbers $a,b>0\in\mathbb{R}$ that the geometric mean x_{g} of a,b equals the geometric mean of the harmonic mean x_{h} of a,b and the arithmetic mean x_{a} of a,b. This means: $x_{\mathrm{g}}=\sqrt{x_{\mathrm{h}}\cdot x_{\mathrm{a}}}$

This can also be shown in the diagram of an right triangle



- 3) Within a manufacturing process on average 75% of the tools are correct.
 - a) Calculate the probability, that within a sample of n = 12 you have exactly 3 correct tools.
 - b) Calculate the probability, that within a sample of n = 9 you have at least 8 correct tools.
 - c) Calculate the expected value, variance and standard variation of a sample of n=25.

- A producer of cocoa knows from experience, that the weight of the 125g-packs is normally distributed with $\mu = 125$ g and variance of $\sigma^2 = 25$ g.
 - a) What is the probability that the weight of a pack is exactly 125 g (argue)?
 - b) What is the probability, that the weight of a pack is within 120 g and 130 g?
 - c) What is the probability, that the weight of a pack is less than 110 g?
 - d) What is the probability, that the weight of a pack is more than 140 g?
 - e) Calculate the symmetric interval around the expected value, such that with a probability of 95% the true weight of a pack is within this interval.
 - f) Sketch your results graphically with the given distribution and the standard normal distribution.
- The annual yield [%] of stock investment can be approximated with a normally distributed random variable with μ =10 and σ =2.
 - a) What is the probability that the yield is within 8% und 14% liegt?
 - b) Assume that the yields oft wo different years are statistically independent.
 - i. What is the probability that the yields in two following years is at least 8%?
 - ii. What is the probability that the yields in the next 10 years will be exactly three times less than 11%?
 - c) Which yield can be maximally expected with a probability of 99%?