Tutorium 1

1. Given are the following two functions:

 $F_1: \quad y = 4 + 3x \qquad F_2: \quad y = 5x$

- (a) Graph both functions in the range $x \ge 0$.
- (b) Calculate the intersection of the two functions by
 - i. equating both sides
 - ii. the Gaussian elimination method
 - iii. the Cramer-rule
- (c) Determine the difference of the two functions $F_2 F_1$ and plot it graphically.
- (d) Interpret the two functions and their difference economically in classical business theory.
- (e) Consider the following general functions

$$F_1: \quad y = a_1 + b_1 x \qquad F_2: \quad y = b_2 x \quad \text{mit } a_1, b_1, b_2 > 0$$

- i. Against the background of the previous economic interpretation, why does one generally demand $a_1, b_1, b_2 > 0$?
- ii. What condition must hold for b_1 and b_2 so that the intersection of both functions is in the positive range?
- iii. Assume that the intersection of F_1 and F_2 is in the positive range. Determine in general the intersection of F_1 and F_2 and investigate the dependence of the intersection on the parameters a_1, b_1, b_2 . Also represent the dependencies graphically.

2. Given is the following time series:

Time	x
2015	103
2016	110
2017	97
2018	105
2019	121

- (a) Determine the arithmetic mean of x.
- (b) Bestimmen Sie die jährlichen Wachstumsraten von x.
- (c) Determine the annual growth rates of x between 2015 and 2019 via
 - i. the arithmetic mean of the annual growth rates
 - ii. the geometric mean of the growth factors. Surprise?
- (d) Give an economic interpretation of the data.
- 3. Given is the following number series:

$$2 + \frac{2}{3} + \frac{2}{9} + \frac{2}{27} + \frac{2}{81} + \dots$$

- (a) How will the series continue?
- (b) What is this type of number series called?
- (c) Calculate the sum $A_4 = 2 + \frac{2}{3} + \frac{2}{9} + \frac{2}{27} + \frac{2}{81}$
- (d) What results if you continue the series to infinity?
- (e) What results in general for the series?

$$A_N = \sum_{n=0}^N q^n \quad \text{or} \quad A_\infty = \sum_{n=0}^\infty q^n \quad 0 < q < 1$$

(f) Give economic applications for this type of number series?